When adding mixed number fractions, what are the main steps?

List all the factors of 20. would you perform?
To estimate the answer to
$1.79 \times 0.0892$, what calculation

A prime number is $\qquad$ .

The general expression for writing a number in standard form is $a \times 10^{b}$. What are the criteria for $a$ and $b$ ?

To divide by a fraction, you multiply by the $\qquad$ of that fraction.

List the first 5 prime numbers.

List all the index laws.

1. Convert them into improper fractions.
2. Multiply to create a common denominator.
3. Add the numerators.
4. Convert the answer back into a mixed number fraction.

## $1,2,4,5,10,20$

A number which has exactly two factors - one and itself.
(Round each number to 1 significant figure.)

## $2,3,5,7,11$

$x^{a} \times x^{b}=x^{a+b}$ (add the powers) $x^{a} \div x^{b}=x^{a-b}$ (subtract the powers)
$\left(x^{a}\right)^{b}=x^{a b}$ (multiply the powers)

$$
\begin{gathered}
x^{0}=1 \\
x^{-a}=\frac{1}{x^{a}} \quad \text { (the reciprocal) } \\
x^{\frac{a}{b}}=(\sqrt[b]{x})^{a} \text { (a root) }
\end{gathered}
$$

$$
1 \leq a<10
$$

$b$ is an integer.

List the steps you would take to work out $12 \%$ of a number without using a calculator.

Write down the decimal multiplier that you would use to work out a $2.5 \%$ increase.

## GCSE Maths Higher Revision Flashcards

A car depreciates by 2\% per annum. It cost $£ 8000$ when it was new. Ben wants to work out how much it would cost after 3 years. Fill in the gap in his calculation. $8000 \times$ $\qquad$ 3

```
GCSE Maths Higher Revision Flashcards
```

To share $£ 72$ in the ratio $2: 7$, you begin by dividing 72 by what number?

State the equations that describe the

1. $y$ is directly proportional to $x$.
2. $y$ is inversely proportional to $x$.
3. $A$ is directly proportional to the square of $r$.
4. $p$ is inversely proportional to the cube root of $q$.

## Q12

The cost of a car service increases by $10 \%$ to $£ 540$. Write down the calculation you would use to work out the cost of the car service before the increase.

List the steps you would take to convert 0.23 to a fraction.

What is the reciprocal of 7 ?

Find $10 \%$ by dividing by 10 .
Find $1 \%$ by dividing by 100 (or dividing the $10 \%$ value by 10 again).

Make $12 \%$ by adding $10 \%$ and $2 \times 1 \%$.

1. Let $x=0.2 \dot{3}$
2. Multiply by 10 and by 100 to get 10x and 100x.
3. Subtract $10 x$ from 100x.
4. Solve this equation for $x$.
e.g.
$100 x=23.3$
$10 x=2.3$
$90 x=21$
$x=\frac{21}{90}=\frac{7}{30}$
5. $y=k x$
6. $y=\frac{k}{x}$
7. $A=k r^{2}$
8. $p=\frac{k}{\sqrt[3]{q}}$

Evaluate:
a. $2^{5}$
b. $7^{2}$
c. $\sqrt{64}$
d. $\sqrt[3]{125}$

GCSE Maths Higher Revision Flashcards

What does it mean to
rationalise the denominator

$$
\text { of } \frac{1}{\sqrt{3}} ?
$$

Which of the following are like terms?

$$
\begin{gathered}
3 x^{2} \\
2 x \\
x^{3} \\
4 x^{6} \\
5 x
\end{gathered}
$$

Explain the process for expanding three brackets such as $(x+1)(x+2)(x+3)$.
Give the general form of an error interval for a number, $x$.

What does factorising mean?

A number, $x$, rounded to 1 decimal place is 2.8. What are the upper and lower bounds of $x$ ?

What is the product rule for counting? ,
a. 32

Upper bound: 2.85
Lower bound: 2.75

This rule says that if there are $m$ ways of choosing one item and $n$ ways of choosing another, the total number of combinations is $m n$.

```
GCSE Maths Higher Revision Flashcards
```

Begin by expanding two brackets using a method like F.O.I.L.

$$
(x+1)(x+2)=x^{2}+3 x+2
$$

Then, multiply each of these terms by each term in the remaining bracket.

$$
\left(x^{2}+3 x+2\right)(x+3)=x^{3}+6 x^{2}+11 x+6
$$

The numerator and denominator of this algebraic fraction have been fully factorised. What is this fraction in its simplest form?

$$
\frac{x^{2}+3 x-10}{x^{2}+10 x+25}=\frac{(x+5)(x-2)}{(x+5)^{2}}
$$

## GCSE Maths Higher Revision Flashcards

## Q27

Find the $n^{\text {th }}$ term of the sequence whose first 4 terms are 1, 5, 9, 13.

List the first two steps required to solve the equation

$$
x^{2}+5 x-1=5
$$

(in a non-calculator exam).

Which inequality is represented on this number line?


What is the 12th term in the sequence with $n^{\text {th }}$ term $4 n+3$ ?

Alex is working out the value of $2 x^{2}$ when $x=3$. He writes the following:

$$
\begin{gathered}
2 \times 3=6 \\
6^{2}=36
\end{gathered}
$$

What is his mistake?

Lily is rearranging a formula to make $x$ the subject. What should her next step be?

$$
\begin{aligned}
& 3 x+r=p-q x \\
& 3 x+r+q x=p \\
& 3 x+q x=p-r
\end{aligned}
$$

## Q32

 $x^{2}+3 x-10>0$. $y=x^{2}+3 x-10$. her inequality?Gaia is solving the inequality

She draws the graph of

What are the solutions to


$$
4 \times 12+3=51
$$

$$
4 n-3
$$

She should factorise $3 x+q x$ to get $x(3+q)$ then she can divide by $(3+q)$.

$$
x<-5 \text { and } x>2
$$

$$
x \leq 8
$$

What do the $m$ and $c$ stand for in the equation for a straight line, $y=m x+c$ ?

A line passes through the point $(0,2)$ and is perpendicular to the line given by $y=\frac{1}{3} x+9$. What is the equation of the line?

Explain how to solve a pair of simultaneous linear equations using the elimination method.

What are the three things you need to remember when working with bearings?

Give the equation of a line that is parallel to $y=4 x+5$.

## Q36

What is the equation to find the gradient of a line passing through two points?

List what you know about angles in parallel lines.

## Q40

The bearing of $A$ from $B$ is $070^{\circ}$. What is the bearing of $B$ from $A$ ?

$$
\begin{aligned}
& y=4 x+a, \text { where } a \text { is any } \\
& \text { number not including } 5 .
\end{aligned}
$$

$m$ is the gradient of the line and $c$ is the value of the $y$-intercept.

$$
y=-3 x+2
$$

Corresponding angles are equal (the ones that look like the letter F).

Alternate angles are equal (the ones that look like the letter Z).

Co-interior/supplementary angles sum to $180^{\circ}$ (the ones that look like the letter C).

A37 1. Make sure the coefficients of either the $x$ or $y$ variables are the same. If not, multiply one or both equations until they are.
2. If the signs of the variable with the same coefficient are the same, subtract the equations. If not, add the equations.
3. Solve this equation.
4. Substitute the answer back into one of the original equations and solve this to find the other variable.

There is always a difference of $180^{\circ}$ in "reverse bearings".

$$
70+180=250^{\circ}
$$

$\frac{\text { change in } y}{\text { change in } x}$ or $\frac{\text { rise }}{\text { run }}$ or $\frac{y_{2}-y_{1}}{x_{2}-x_{1}}$

1. Measure from the North line.
2. Measure in a clockwise direction.
3. Use 3 digits, e.g. $83^{\circ}$ would be $083^{\circ}$.

What is the formula to calculate the sum of the interior angles (in degrees) in an $n$-sided polygon?

GCSE Maths Higher Revision Flashcards

## Q43

What is a bisector?

State the formulae for the area and circumference of a circle.

What is the formula for the volume of a prism?

What is the sum of the exterior angles of a polygon?

What is the formula for the area of a trapezium?

State the formulae for the arc length and area of a sector with an angle of $\theta^{\circ}$.

## Q48

How could you use Pythagoras' theorem to prove that a triangle with dimensions $6 \mathrm{~cm}, 8 \mathrm{~cm}$ and 10 cm is right-angled?

A bisector is a line that cuts another line or an angle in half. We construct bisectors using a ruler and a pair of compasses (and a pencil).

$$
\text { Area }=\pi r^{2}
$$

Circumference $=\pi d$ or $2 \pi r$

Find the sum of the squares of the smaller sides.

$$
6^{2}+8^{2}=100
$$

Square the remaining side.

$$
10^{2}=100
$$

Since these are equal, this triangle satisfies Pythagoras' theorem and must be right-angled.

Volume $=$ area of cross-section $\times$ length

Rearrange the equation for the cosine rule to make $\cos \theta$ the subject:

$$
a^{2}=b^{2}+c^{2}-2 b c \cos \theta
$$

State the values of:
a. $\sin 60^{\circ}$
b. $\cos 45^{\circ}$
c. $\tan 30^{\circ}$

A shape has been translated by a vector $\binom{3}{2}$. What does this look like?

What does a negative scale factor for enlargement look like?

## Q56

Two cylinders, $A$ and $B$, are similar. The radius of cylinder $A$ is 8 cm . The radius of cylinder $B$ is 16 cm .

The volume of cylinder $A$ is $12 \mathrm{~cm}^{3}$. What is the volume of cylinder B?

$$
\cos \theta=\frac{b^{2}+c^{2}-a^{2}}{2 b c}
$$

a. $\frac{\sqrt{3}}{2}$
b. $\frac{\sqrt{2}}{2}$
C. $\frac{\sqrt{3}}{3}$ or $\frac{1}{\sqrt{3}}$

1. centre of rotation
2. angle
3. direction

The shape slides 3 units right and 2 units up.

Length scale factor $=\frac{16}{8}=2$
Volume scale factor $=2^{3}=8$
Volume $B=8 \times 12=96 \mathrm{~cm}^{3}$
The enlargement appears on the other side of the centre of enlargement.

Q57 The diagram shows a circle with a triangle inscribed in it. Angle $C A B=32^{\circ}$ and angle $A B C=48^{\circ}$. Is $A B$ the diameter of the circle? Explain your answer.


Diagram NOT accurately drawn
GCSE Maths Higher Revision Flashcards

Which circle theorem can be applied to this diagram?


GCSE Maths Higher Revision Flashcards

Write as a single vector:

$$
\binom{1}{5}-3\binom{2}{-2}
$$

A car travels at 45 mph for 20 minutes. What calculation would you perform to find the distance travelled in miles?

Q58 Which circle theorem can be applied to this diagram?


What is the trigonometric formula for the area of a triangle?

What does the area between a speed-time graph and the $x$-axis represent?

## Q64

The mass of a block is 100 g and its volume is $25 \mathrm{~cm}^{3}$. What is its density? Give the units to your answer.

Angles in a triangle add to $180^{\circ}$. Angle ACB = $180-(32+48)=100^{\circ}$ No, angles in a semi-circle are $90^{\circ}$ and $90 \neq 100$ so $A B$ is not the diameter of the circle.

Alternate segment theorem

$$
\frac{1}{2} a b \sin C
$$

The distance travelled.

Density $=\frac{100}{25}=4 \mathrm{~g} / \mathrm{cm}^{3}$

What is the formula for pressure?

## Q67

What does it mean for a point to be invariant under a transformation?

What kind of data is a two-way table used to present?

What are the types of correlation that can be represented in a scatter graph?

List the four criteria for proving congruency in triangles.

## Q68

What are the missing numbers in this frequency tree?


List the steps required to draw a pie chart.

## Q72

What is the formula for frequency density?

SSS, ASA, SAS, RHS

What are the missing numbers in this


GCSE Maths Higher Revision Flashcards
BEYOND GCSE Maths Higher Revision Flashcards

BEYOND

## A69

1. Find the total frequency.
2. Divide 360 by this number.
3. Multiply each frequency by this new number.
4. Draw each angle carefully and label each sector.

Frequency density $=\frac{\text { frequency }}{\text { class width }}$

Bivariate data - data that uses two variables.

Positive correlation - as one variable increases, so does the other.
Negative correlation - as one variable decreases, the other increases.

No correlation - there is no clear relationship between the variables.

BEYOND

## A71

How can you quickly calculate the frequency from a bar on a histogram?

Label the box plot diagram.
 GCSE Maths Higher Revision Flashcards
the mean from this frequency table?

| Age, $x$, years | Frequency |
| :---: | :---: |
| $0 \leq x<10$ | 3 |
| $10 \leq x<20$ | 4 |
| $20 \leq x<30$ | 7 |
| $30 \leq x<40$ | 1 |

What does it mean for two events to be mutually exclusive?

Use the midpoint of each interval.

Label the box plot diagram.

$$
P(A \text { and } B)=P(A) \times P(B)
$$

The events cannot occur at the same time.

Work out its area.

Use the end point of each interval.

Find the midpoints of the intervals.
Multiply these values by the frequency to calculate $f x$.
Divide the sum of these values by the total frequency: $\frac{\sum f x}{\sum f}$

The probability of (A union $B$ ), which is the probability of $A$, or $B$, or both occurring.

A circle has equation $x^{2}+y^{2}=4$. Describe the circle.

What does $\mathrm{P}(\mathrm{A} \cap \mathrm{B})$ mean?

$$
f(x)=4 x \text { and } g(x)=x+5 .
$$

What is $f g(x)$ ?
f two lines are perpendicular, what can we say about their gradients?

List the steps for finding the inverse $f^{-1}(x)$ of a function $f(x)$.

## Q88 Fill in the gaps:

To sketch the graph of $y=x^{2}+5 x+4$, begin by factorising the expression $x^{2}+5 x+4$ to get the following:
$y=(x+4)(x+1)$

State the equation of a line whose gradient is -2 and which passes through $(0,3)$.

What does P(A') mean?

Solving $(x+4)(x+1)=0$ gives $x=-4$ and $x=-1$ which are the $\qquad$ of the graph.

The graph passes through the $y$-axis at $\qquad$ .

$$
y=-2 x+3
$$

A circle, centred at $(0,0)$, with a radius of $\sqrt{4}=2$ units.

The probability of (A intersection B), which is the probability of A and B occurring. In a Venn diagram, it represents the overlap.

## A85

$$
\begin{aligned}
f g(x) & =f(g(x)) \\
& =f(x+5) \\
& =4(x+5) \\
& =4 x+20
\end{aligned}
$$

The product of the gradients is -1 (when we multiply them together, we get-1).

Alternatively, the gradients will be the "negative reciprocal" of one another.

Write the equation as $y=f(x)$.
Switch the $y$ and the $x$.
Make $y$ the subject.
This equation is now the inverse function. this graph represent?


GCSE Maths Higher Revision Flashcards

## Q91

The graph of $y=2^{x}$ passes through the $y$-axis at $\qquad$ _

What is the quadratic formula for an equation of the form

$$
a x^{2}+b x+c=0 ?
$$

Describe the transformation that maps the graph of $y=f(x)$ onto the graph of $y=f(x+1)$.

## Q90

What are the $x$ - and $y$-intercepts of the graph of $y=\cos (x)$ for $0 \leq x \leq 360^{\circ}$ ?

## Q92

Use algebra to describe the following:

- An even number
- An odd number
- Three consecutive integers
- A multiple of 5

A quadratic equation in completed square form is $y=(x-3)^{2}+2$. What is the coordinate of the turning point of its graph?

## Q96

Describe the transformation that maps the graph of $y=f(x)$ onto the graph of $y=f(x)+3$.
$y$-intercept $=1$
$x$-intercepts $=90^{\circ}$ and $270^{\circ}$

- An even number is $2 n$
- An odd number is $2 n+1$
- Three consecutive integers are $n, n+1$ and $n+2$
- A multiple of 5 is $5 n$
$(3,2)$

A translation by $\binom{0}{3}$.

An iterative formula is given as

$$
x_{(n+1)}=\frac{2}{x_{n}}-8 .
$$

If $x_{0}=3$, explain how you would calculate $x_{1}$.

Substitute $x_{0}=3$ into the formula:

$$
x_{1}=\frac{2}{3}-8
$$

